

## ERRATUM TO “KOSZUL DUALITY FOR OPERADS”

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In Section 2.2 of our paper “Koszul Duality for Operads” [1], the definition of the products  $\bullet, \circ$  was given incorrectly. It should be replaced by the following.

For any two  $\Sigma_2$ -modules  $V, W$  we have maps

$$\phi_n: F(V \otimes W)(n) \hookrightarrow F(V)(n) \otimes F(W)(n),$$

$$\psi_n: F(V)(n) \otimes F(W)(n) \rightarrow F(V \otimes W)(n).$$

The  $\phi_n$  come from a morphism of operads  $\phi = \phi_{V,W}: F(V \otimes W) \hookrightarrow F(V) \otimes F(W)$ , which reflects the fact that the tensor product of an  $F(V)$ -algebra and an  $F(W)$ -algebra is an  $F(V \otimes W)$ -algebra. The map  $\psi_n$  is dual to  $\phi_{V,W,n}$ .

Now, given two quadratic operads  $\mathcal{P}, \mathcal{Q}$  with  $\mathcal{P}(2) = V, \mathcal{Q}(2) = W$  and spaces of relations  $R_{\mathcal{P}}, R_{\mathcal{Q}}$ , the spaces of relations of  $\mathcal{P} \circ \mathcal{Q}$  and  $\mathcal{P} \bullet \mathcal{Q}$  should be defined, respectively, as

$$\phi_3^{-1}((R_{\mathcal{P}} \otimes F(W)(3)) + (F(V)(3) \otimes R_{\mathcal{Q}})),$$

$$\psi_3((R_{\mathcal{P}} \otimes F(W)(3)) \cap (F(V)(3) \otimes R_{\mathcal{Q}})).$$

All the results of Section 2.2 are valid with these definitions of the products.

We would like to thank G. Bergman for bringing this matter to our attention.

## REFERENCES

- [1] V. GINZBURG AND M. KAPRANOV, *Koszul duality for operads*, *Duke Math. J.* **76** (1994), 203–273.

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